

**COORDINATE GEOMETRY WS 4**

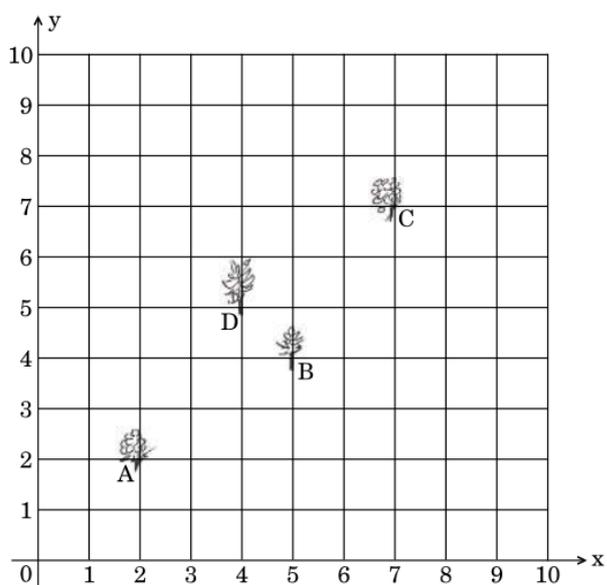
**Class 10 - Mathematics**

1. If a point A (0, 2) is equidistant from the points B(3, p) and C(p, 5), then find the value of p. [2]
2. Find the distance between the points (0, 0) and (36, 15). [2]
3. Find the distance between the points (0, 0) and (36, 15). Also, find the distance between towns A and B if town B is located at 36 km east and 15 km north of town A. (In km) [2]
4. Find a point on y-axis which is equidistant from the points (5, -2) and (-3, 2). [2]
5. Find the distance of A(5, -12) points from the origin. [2]
6. Match the following: [2]

(a) The point lies above the x-axis	(i) (0, 3)
(b) The point lies on the x-axis	(ii) (-1, 2)
(c) The point lies on y-axis	(iii) (3, 5)
(d) The point lies to the right of the y-axis	(iv) (2, 0)

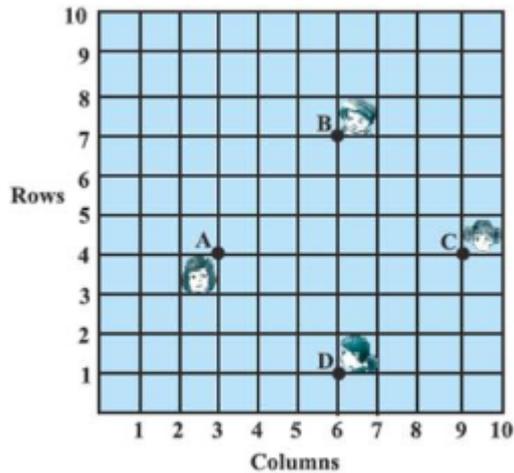
7. Find the fourth vertex of a rectangle whose three vertices taken in order are (4, 1), (7, 4) and (13, -2). [2]
8. Find the points on the x-axis, each of which is at a distance of 10 units from the point A(11, -8). [2]
9. Point P(x, y) is equidistant from the points A(5, 1) and B(1, 5), prove that  $x = y$ . [2]
10. Name the type of triangle PQR formed by the points P ( $\sqrt{2}$ ,  $\sqrt{2}$ ), Q ( $-\sqrt{2}$ ,  $-\sqrt{2}$ ) and R ( $-\sqrt{6}$ ,  $\sqrt{6}$ ). [2]
11. Find the value of a, if the distance between the points A (-3, -14) and B (a, -5) is 9 units. [2]
12. If A(4, 3), B (-1, y), and C(3, 4) are the vertices of a right triangle ABC, right angled at A, then find the value of y. [2]
13. Find a point on the y-axis which is equidistant from the points A(6, 5) and B (-4, 3). [2]
14. Find the values of x for which the distance between the points P(x, 4) and Q(9,10) is 10 units. [2]
15. Find the point on x-axis which is equidistant from the points (-2, 5) and (2, -3). [2]
16. What is the distance between the points (5 sin 60°, 0) and (0, 5 sin 30°)? [2]
17. If the distance between points (x, 0) and (0,3) is 5, what are the values of x? [2]
18. Name the type of quadrilateral formed, if any, by the points (4, 5), (7, 6), (4, 3), (1, 2), and give a reason for your answer. [2]
19. Find the distance between the points A (7,13) and B(10,9). [2]
20. Show that the points (-2, 3), (8, 3) and (6, 7) are the vertices of a right-angled triangle. [2]
21. Prove that the points A(-1, 0), B(3, 1), C(2, 2) and D(-2, 1) are the vertices of a parallelogram ABCD. Is it also a rectangle? [2]
22. The base PQ of two equilateral triangles PQR and PQR' with side '2a' lies along y-axis such that the mid-point of PQ is at the origin. Find the coordinates of the vertices R and R' of the triangles. [2]
23. Find the relation between x and y such that the point (x, y) is equidistant from the points (7, 1) and (3, 5). [2]
24. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4). [2]
25. Check whether the points (20, 3), (19, 8) and (2, -9) are all equidistant from the point (7, 3). [2]

26. If  $Q(0, 1)$  is equidistant from  $P(5, -3)$  and  $R(x, 6)$ , find the values of  $x$ . [2]
27. If  $Q(0, 1)$  is equidistant from  $P(5, -3)$  and  $R(x, 6)$ , find the values of  $x$ . Also find the distances  $QR$  and  $PR$ . [2]
28. Check whether the points  $P(5, -2)$ ,  $Q(6, 4)$  and  $R(7, -2)$  are the vertices of an isosceles triangle  $PQR$ . [2]
29. Find the values of  $x$  for which the distance between the points  $A(x, 2)$  and  $B(9, 8)$  is 10 units. [2]
30. Show that the points  $A(1, -2)$ ,  $B(3, 6)$ ,  $C(5, 10)$  and  $D(3, 2)$  are the vertices of a parallelogram. [2]
31. Find the point on  $x$ -axis which is equidistant from the points  $(5, -2)$  and  $(-3, 2)$ . [2]
32.  $A(-2, 2)$ ,  $B(5, 2)$  and  $C(k, 8)$  are the vertices of a right-angled triangle  $ABC$  with  $\angle B = 90^\circ$ , then find the value of  $k$ . [2]
33. Find the distance between the points  $(0, 0)$  and  $(36, 15)$ . Also, find the distance between towns  $A$  and  $B$  if town  $B$  is located at 36 km east and 15 km north of town  $A$ . [2]
34. Find the distance of the point  $P(6, -6)$  from the origin. [2]
35. Find the distance between the points:  
 $A(-6, -4)$  and  $B(9, -12)$  [2]
36. Two vertices of a  $\triangle ABC$  are given by  $A(6, 4)$  and  $B(-2, 2)$ , and its centroid is  $G(3, 4)$ . Find the coordinates of the third vertex  $C$  of  $\triangle ABC$ . [2]
37. Find the perimeter of a triangle with vertices  $(0, 0)$ ,  $(1, 0)$  and  $(0, 1)$ . [2]
38. Find the value(s) of  $x$  so that  $PQ = QR$ , where the coordinates of  $P$ ,  $Q$  and  $R$  are  $(6, -1)$ ,  $(1, 3)$  and  $(x, 8)$  respectively. [2]
39. If  $P(x, y)$  is a point equidistant from the points  $A(6, -1)$  and  $B(2, 3)$ , show that  $x - y = 3$ . [2]
40. Do the points  $(3, 2)$ ,  $(-2, -3)$  and  $(2, 3)$  form a triangle? If so, name the type of triangle formed. [2]
41. Find the values of  $y$  for which the distance between the points  $P(2, -3)$  and  $Q(10, y)$  is 10 units. [2]
42. Krishna has an apple orchard which has a  $10\text{ m} \times 10\text{ m}$  sized kitchen garden attached to it. She divides it into a  $10 \times 10$  grid and puts soil and manure into it. She grows a lemon plant at  $A$ , a coriander plant at  $B$ , an onion plant at  $C$  and a tomato plant at  $D$ . Her husband Ram praised her kitchen garden and points out that on joining  $A$ ,  $B$ ,  $C$  and  $D$  they may form a parallelogram. Look at the below figure carefully and answer the following questions: [2]

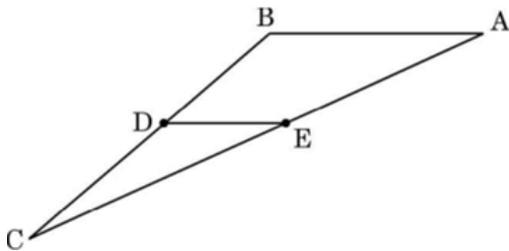


- i. Write the coordinates of the points  $A$ ,  $B$ ,  $C$ , and  $D$ , using the  $10 \times 10$  grid as coordinate axes.
- ii. Find whether  $ABCD$  is a parallelogram or not
43. Find the value(s) of  $y$  for which the distance between the points  $A(3, -1)$  and  $B(11, y)$  is 10 units. [2]
44. Find all possible values of  $x$  for which the distance between the points  $A(x, -1)$  and  $B(5, 3)$  is 5 units. [2]

45. Find a relation between  $x$  and  $y$  such that the point  $(x, y)$  is equidistant from the points  $(7, 1)$  and  $(3, 5)$ . [2]
46. Find the distance between the points: [2]  
 $P(a \sin \alpha, a \cos \alpha)$  and  $Q(a \cos \alpha, -a \sin \alpha)$
47. In a classroom, 4 friends are seated at the four points A, B, C and D as shown in Fig. Champa and Chameli walk [2]  
 into the class and after observing for a few minutes Champa asks Chameli, Don't you think ABCD is a square?  
 Chameli disagrees. Using distance formula, find which of them is correct.



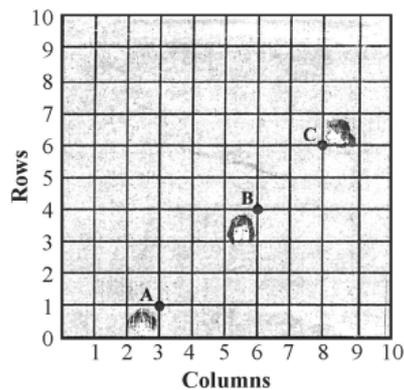
48. Determine if the points  $(1, 5)$ ,  $(2, 3)$  and  $(-2, -11)$  are collinear. [2]
49. Find the distance between the pair of points  $(a, b)$ ,  $(-a, -b)$  [2]
50. Prove that in a right-angled triangle, the mid-point of the hypotenuse is equidistant from the vertices. [2]
51. Prove that points  $(0,0)$ ,  $(5,5)$  and  $(-5,5)$  are vertices of a right-angled isosceles triangle. [2]
52. The points A  $(2, 0)$ , B  $(9, 1)$ , C  $(11, 6)$  and D  $(4, 4)$  are the vertices of a quadrilateral ABCD. Determine whether [2]  
 ABCD is a rhombus or not.
53. In the given figure, in  $\triangle ABC$  points D and E are mid-points of sides BC and AC respectively. If given vertices [2]  
 are A $(4, -2)$ , B $(2, -2)$  and C $(-6, -7)$ , then verify the result  $DE = \frac{1}{2} AB$ .



54. Find the distance of C $(-4, -6)$  points from the origin. [2]
55. Find the lengths of the medians AD and BE of  $\triangle ABC$  whose vertices are A $(7, -3)$ , B $(5, 3)$  and C $(3, -1)$ . [2]
56. Find the distance between the points  $(0, 0)$  and  $(36, 15)$ . [2]
57. If A $(3, y)$  is equidistant from points P $(8, -3)$  and Q $(7, 6)$ , find the value of  $y$  and find the distance AQ. [2]
58. Check whether  $(5, -2)$ ,  $(6, 4)$  and  $(7, -2)$  are the vertices of an isosceles triangle. [2]
59. Find the distance between the points: [2]  
 $A(7, -4)$  and  $B(-5, 1)$ .
60. If the distance between the points  $(3, 0)$  and  $(0, y)$  is 5 units and  $y$  is positive, then what is the value of  $y$ ? [2]
61. Write the perimeter of the triangle formed by the points O  $(0,0)$ , A  $(a, 0)$  and B  $(0, b)$ . [2]
62. Find the distance between the points A  $(at_1^2, 2at_1)$  and B  $(at_2^2, 2at_2)$  [2]
63. Determine, by distance formula, whether the given points are collinear :  $(1, 2)$ ,  $(5, 3)$  and  $(18, 6)$ . [2]
64. Use analytical geometry to prove that the mid-point of the hypotenuse of a right-angled triangle is equidistant [2]  
 from its vertices.

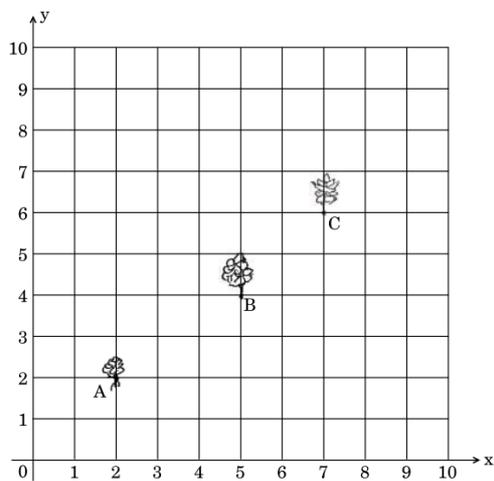
65. In the figure, the arrangement of desks in a classroom is shown. Ashima, Bharti, and Asha are seated at A, B, and C respectively. Answer the following: [2]

- i. Find whether the girls are sitting in a line.
- ii. If A, B, and C are collinear, find the ratio in which point B divides the line segment joining A and C.



66. AOBC is a rectangle whose three vertices are A(0,3), O(0, 0) and B(5, 0). Find the length of its diagonal. [2]
67. If a point A (0,2) is equidistant from the points B(3,p) and C(p, 5), then find the value of p. [2]
68. Show that the points (7, 10), (-2, 5) and (3, -4) are the vertices of an isosceles right triangle. [2]
69. Find the point on the x-axis which is equidistant from (2, -5) and (-2, 9). [2]
70. If the points A(-1, y) and B(5, 7) lie on a circle with centre O(2, -3y), then find the values of y. [2]
71. Show that A(-3, 2), B(-5, -5), C(2, -3) and D(4, 4) are the vertices of a rhombus. [2]
72. Seema has a 10 m × 10 m kitchen garden attached to her kitchen. She divides it into a 10 × 10 grid and wants to grow some vegetables and herbs used in the kitchen. She puts some soil and manure in that and sows a green chilly plant at A, a coriander plant at B and a tomato plant at C. [2]

Her friend Kusum visited the garden and praised the plants grown there. She pointed out that they seem to be in a straight line. See the below diagram carefully and answer the following questions :



- i. Write the coordinates of the points A, B, and C taking the 10 × 10 grid as coordinate axes.
  - ii. By distance formula or some other formula, check whether the points are collinear.
73. Determine whether the given points are vertices of a right triangle: (-2, 1), (2 -2), and (5, 2) [2]
74. If the points (2, 1) and (1,-2) are equidistant from the point (x, y), show that  $x + 3y = 0$ . [2]
75. If A (-3, 2), B(p, q) and C(-1, 4) are the vertices of an isosceles triangle, show that  $p + q = 1$ , if  $AB = BC$ . [2]